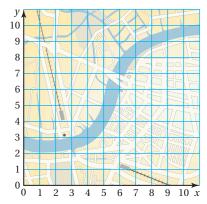
4.4 Polygons in the Coordinate Plane

Essential Question How can you find the lengths of line segments in a coordinate plane?

1 ACTIVITY: Finding Distances on a Map

Work with a partner. The coordinate grid shows a portion of a city. Each square on the grid represents one square mile.



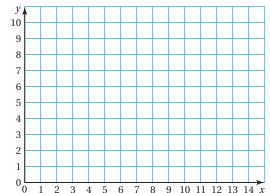
- **a.** A public library is located at (4, 5). City Hall is located at (7, 5). Plot and label these points.
- **b.** How far is the public library from City Hall?
- **c.** A stadium is located 4 miles from the public library. Give the coordinates of several possible locations of the stadium. Justify your answers by graphing.
- **d.** Connect the three locations of the public library, City Hall, and the stadium using your answers in part (c). What shapes are formed?

2 ACTIVITY: Graphing Polygons

Work with a partner. Plot and label each set of points in the coordinate plane. Then connect each set of points to form a polygon.

Rectangle: A(2, 3), B(2, 10), C(6, 10), D(6, 3)

Triangle: E(8, 3), F(14, 8), G(14, 3)



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In this lesson, you will

- draw polygons in the coordinate plane.
- find distances in the coordinate plane.
- solve real-life problems.

ACTIVITY: Finding Distances in a Coordinate Plane

Work with a partner.

Math

Practice

CalculationsWhat calculations

are repeated? How

can you use this

information to write a rule about

the length of a

line segment?

Repeat

- **a.** Find the length of each horizontal line segment in Activity 2.
- **b. STRUCTURE** What relationship do you notice between the lengths of the line segments in part (a) and the coordinates of their endpoints? Explain.
- **c.** Find the length of each vertical line segment in Activity 2.
- **d. STRUCTURE** What relationship do you notice between the lengths of the line segments in part (c) and the coordinates of their endpoints? Explain.
- **e.** Plot and label the points below in the coordinate plane. Then connect each pair of points with a line segment. Use the relationships you discovered in parts (b) and (d) above to find the length of each line segment. Show your work.

S(3, 1) and T(14, 1) U(9, 8) and V(9, 0) W(0, 7) and X(0, 10) Y(1, 9) and Z(7, 9)

f. Check your answers in part (e) by counting grid lines.

b.

-What Is Your Answer?

- **4. IN YOUR OWN WORDS** How can you find the lengths of line segments in a coordinate plane? Give examples to support your explanation.
- **5.** Do the methods you used in Activity 3 work for diagonal line segments? Explain why or why not.
- **6.** Use the Internet or some other reference to find an example of how "finding distances in a coordinate plane" is helpful in each of the following careers.

a.



Archaeologist



Surveyor



Pilot



Use what you learned about finding the lengths of line segments to complete Exercises 3–5 on page 178.



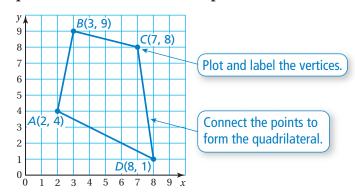
You can use ordered pairs to represent vertices of polygons. To draw a polygon in a coordinate plane, plot and connect the ordered pairs.

EXAMPLE

Drawing a Polygon in a Coordinate Plane

The vertices of a quadrilateral are A(2,4), B(3,9), C(7,8), and D(8,1). Draw the quadrilateral in a coordinate plane.

Study Tip After you plot the vertices, connect them in order to draw the polygon.



On Your Own



Draw the polygon with the given vertices in a coordinate plane.

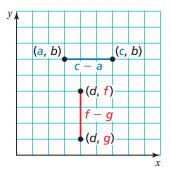
- **1.** A(0, 0), B(5, 7), C(7, 4)
- **2.** *W*(4, 4), *X*(7, 4), *Y*(7, 1), *Z*(4, 1)
- **3.** F(1,3), G(3,6), H(5,6), J(3,3)
- **4.** $P(1, 4), Q(3, 5), R(7, 3), S\left(6, \frac{1}{2}\right), T\left(2, \frac{1}{2}\right)$



Finding Distances in the First Quadrant

You can find the length of a horizontal or vertical line segment in a coordinate plane by using the coordinates of the endpoints.

- When the x-coordinates are the same, the vertical distance between the points is the difference of the *y*-coordinates.
- When the *y*-coordinates are the same, the horizontal distance between the points is the difference of the *x*-coordinates.



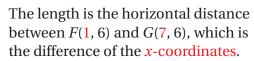
Be sure to subtract the lesser coordinate from the greater coordinate.

The vertices of a rectangle are F(1,6), G(7,6), H(7,2), and J(1,2). Draw the rectangle in a coordinate plane and find its perimeter.

Draw the rectangle and use the vertices to find its dimensions.

Study Tip

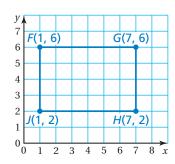
You can also find the length using vertices *H* and *J*. You can find the width using vertices *F* and *J*.



length =
$$7 - 1 = 6$$
 units

The width is the vertical distance between G(7, 6) and H(7, 2), which is the difference of the *y*-coordinates.

width =
$$6 - 2 = 4$$
 units



So, the perimeter of the rectangle is 2(6) + 2(4) = 20 units.



Real-Life Application

In a grid of the exhibits at a zoo, the vertices of the giraffe exhibit are E(0, 90), F(60, 90), G(100, 30), and H(0, 30). The coordinates are measured in feet. What is the area of the giraffe exhibit?

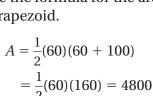
Plot and connect the vertices using a coordinate grid to form a trapezoid. Use the coordinates to find the lengths of the bases and the height.

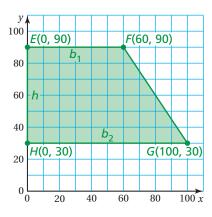
$$b_1 = 60 - 0 = 60$$

$$b_2 = 100 - 0 = 100$$

$$h = 90 - 30 = 60$$

Use the formula for the area of a trapezoid.





You can count grid lines to find the dimensions, but make sure you consider the scale of

Common Error

the axes.

The area of the giraffe exhibit is 4800 square feet.



On Your Own



- **5.** The vertices of a rectangle are J(2, 7), K(4, 7), L(4, 1.5), and M(2, 1.5). Find the perimeter and the area of the rectangle.
- **6. WHAT IF?** In Example 3, the giraffe exhibit is enlarged by moving vertex F to (80, 90). How does this affect the area? Explain.

4.4 Exercises





Vocabulary and Concept Check

- 1. WRITING How can you use a coordinate plane to draw a polygon?
- **2. WRITING** How can you find the perimeter of a rectangle in a coordinate plane?



Practice and Problem Solving

Plot and label each pair of points in a coordinate plane. Find the length of the line segment connecting the points.

Draw the polygon with the given vertices in a coordinate plane.

7.
$$D(\frac{1}{2}, 2), E(5, 5), F(4, 1)$$

8.
$$G\left(1\frac{1}{2}, 4\right), H\left(1\frac{1}{2}, 8\right), J(5, 8), K(5, 4)$$

9.
$$L(3, 2), M(3, 5), N(9, 5), P(9, 2)$$

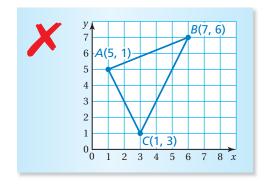
11.
$$V(2, 2), W(3, 7\frac{1}{2}), X(8, 7\frac{1}{2}), Y(10, 4), Z(7, 0)$$

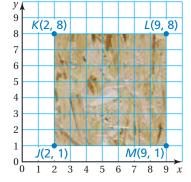
Find the perimeter and the area of the polygon with the given vertices.

13.
$$J(1, 2), K(7, 2), L(7, 8), M(1, 8)$$

14.
$$N(0, 2), P(5, 2), Q(5, 5), R(0, 5)$$

16. ERROR ANALYSIS Describe and correct the error in drawing a triangle with vertices A(5, 1), B(7, 6), and C(1, 3).

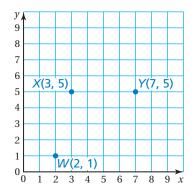




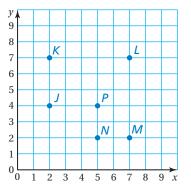
- **17. TREE HOUSE** You design a tree house using a coordinate plane. You plot the vertices of the floor at J(2, 1), K(2, 8), L(9, 8), and M(9, 1). The coordinates are measured in feet.
 - **a.** What is the shape of the floor?
 - **b.** What are the perimeter and the area of the floor?

OPEN-ENDED Draw a polygon with the given conditions in a coordinate plane.

- **18.** a square with a perimeter of 20 units
- **20.** a rectangle with an area of 24 units²
- **22. STRUCTURE** The coordinate plane shows three vertices of a parallelogram. Find two possible points that could represent the fourth vertex.



- **19.** a rectangle with a perimeter of 18 units
- 21. a triangle with an area of 15 units²
- **23. BUS ROUTE** Polygon *JKLMNP* represents a bus route. Each grid square represents 9 square miles. What is the shortest distance, in miles, from station P to station L using the bus route? Explain your reasoning.





- 24. CITY LIMITS In a topographical map of a city, the vertices of the city limits are A(10, 9), B(18, 9), C(18, 2), D(14, 4.5), and E(10, 4.5). The coordinates are measured in miles. What is the area of the city?
- **25. BACKYARD** The vertices of a backyard are W(10, 30), X(10, 100), Y(110, 100), and Z(50, 30). The coordinates are measured in feet. The line segment XZ separates the backyard into a lawn and a garden. The area of the lawn is greater than the area of the garden. How many times larger is the lawn than the garden?
- **26.** Precision The vertices of a rectangle are (1, 0), (1, a), (5, a), and (5, 0). The vertices of a parallelogram are (1, 0), (2, b), (6, b), and (5, 0). The value of a is greater than the value of b. Which polygon has a greater area? Explain your reasoning.



Fair Game Review What you learned in previous grades & lessons

Divide. Write the answer in simplest form. (Section 2.3)

- **27.** $1\frac{1}{3} \div \frac{2}{3}$

- **28.** $6\frac{3}{5} \div \frac{3}{4}$ **29.** $2\frac{1}{2} \div 8$ **30.** $4\frac{1}{6} \div 1\frac{1}{8}$
- **31. MULTIPLE CHOICE** You are filling bottles from 5 gallons of lemonade. How many bottles can you fill when each bottle is $\frac{3}{8}$ of a gallon? (Section 2.2)
- **B** 3

- **©** 8
- **D** $13\frac{1}{2}$